

# COMPARATIVE STUDY OF THE HADRONIC PRODUCTION OF $B_c$ MESONS\*

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## Abstract

The full order  $\alpha_s^4$  perturbative QCD calculation of the production of  $B_c$  mesons at the Tevatron is compared with the fragmentation approximation. The non-fragmentation diagrams, in which two or more quarks and/or gluons can simultaneously be nearly on-shell, are important unless  $P_T \gg M_{B_c}$ .

## I. INTRODUCTION

Hadronic production of  $B_c$  and  $B_c^*$  mesons is of considerable, current interest. At hadronic colliders, the dominant subprocess is  $g + g \rightarrow B_c(B_c^*) + b + \bar{c}$  and 36 Feynman diagrams contribute in the lowest order,  $\alpha_s^4$ . At sufficiently large  $B_c$  or  $B_c^*$  transverse momentum,  $P_T$ , the fragmentation approximation dominates. This process is ideal for quantitatively comparing the fragmentation approximation and the full order  $\alpha_s^4$  calculation, since both can be reliably calculated. We have shown [1] that the fragmentation approximation

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and the full order  $\alpha_s^4$  calculation agree when and only when  $P_T \gg M_{B_c}$ . At small  $P_T$  the non-fragmentation contributions become important since, when the  $B_c$  or  $B_c^*$  is nearly collinear with the initial partons, it is possible for two or more quarks and/or gluons in the subprocesses to simultaneously be nearly on-mass-shell.

## II. CALCULATIONS AND RESULTS

Figure 1 shows the  $P_T$  distributions for the process  $p + \bar{p} \rightarrow B_c(B_c^*) + X$  at the Fermilab Tevatron energy  $\sqrt{s} = 1.8$  TeV with the rapidity cut  $|Y| < 1.5$ . Remarkably, the  $B_c$  meson  $P_T$  distributions agree rather well, even for  $P_T$  as small as about 5 GeV, while for the  $B_c^*$  meson the distributions differ by 50–70% over a much larger range of  $P_T$ , leaving the comparison inconclusive.

The  $P_T$  distributions for the subprocess  $g(k_1) + g(k_2) \rightarrow B_c(P) + b(q_2) + \bar{c}(q_1)$ , which are shown in Fig. 2, are somewhat more revealing. The distributions agree reasonable well when  $P_T$  is larger than about 30 GeV for the  $B_c$  meson and about 40 GeV for the  $B_c^*$  meson. Consequently, the  $P_T$  distributions alone are not decisive and, as will be shown, can even be misleading.

It is more insightful to examine the distributions in  $z = 2(k_1 + k_2) \cdot P/\hat{s}$ , which is simply twice the fraction of the total energy carried by the  $B_c$  or  $B_c^*$  in the subprocess center of mass. Note that  $z$  is experimentally measurable, at least in principle. Figure 3 shows the  $z$  distributions,  $C(z)$ , for the process  $p + \bar{p} \rightarrow B_c(B_c^*) + X$  for  $\sqrt{s} = 1.8$  TeV,  $|Y| < 1.5$ , and  $P_T > 10$  GeV. The distribution [1]  $C(z) \equiv d\sigma/dz$ . From Fig. 3 it is clear that for the  $B_c$  the fragmentation approximation underestimates the full order  $\alpha_s^4$  calculation for small  $z$  and overestimates it for large  $z$ . This results in a cancelation in the  $B_c$   $P_T$  distribution, Fig. 1, fortuitously causing the fragmentation approximation to agree with the full order  $\alpha_s^4$  calculation down to quite small values of  $P_T$ .

However, for the  $B_c^*$  the fragmentation calculation underestimates the full order  $\alpha_s^4$  calculation at all values of  $z$  and no fortuitous cancelation occurs, as for the  $B_c$ .

The relative importance of the fragmentation and non-fragmentation contributions is even more clearly evident in the  $P_T$  distributions for the subprocess  $g + g \rightarrow B_c(B_c^*) + b + \bar{c}$  at very large  $\sqrt{\hat{s}}$ , as is shown in Fig. 4. Clearly, the non-fragmentation contributions dominate at small  $P_T$ , where two or more quarks and/or gluons can simultaneously be very nearly on-mass-shell in the subprocess.

### III. CONCLUSIONS

We have compared the full order  $\alpha_s^4$  perturbative QCD calculation of the production of  $B_c$  and  $B_c^*$  mesons at the Fermilab Tevatron with the fragmentation approximation. There are Feynman diagrams present in the full order  $\alpha_s^4$  matrix element in which *two or more* quarks and/or gluons can simultaneously be nearly on-mass-shell, and these dominate over the fragmentation approximation at small  $P_T$ . The fragmentation approximation dominates when and only when  $P_T \gg M_{B_c}$ .

### ACKNOWLEDGMENTS

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## REFERENCES

- [1] C.H. Chang, Y.Q. Chen, and R.J. Oakes, Phys. Rev. D, in press.

# FIGURES

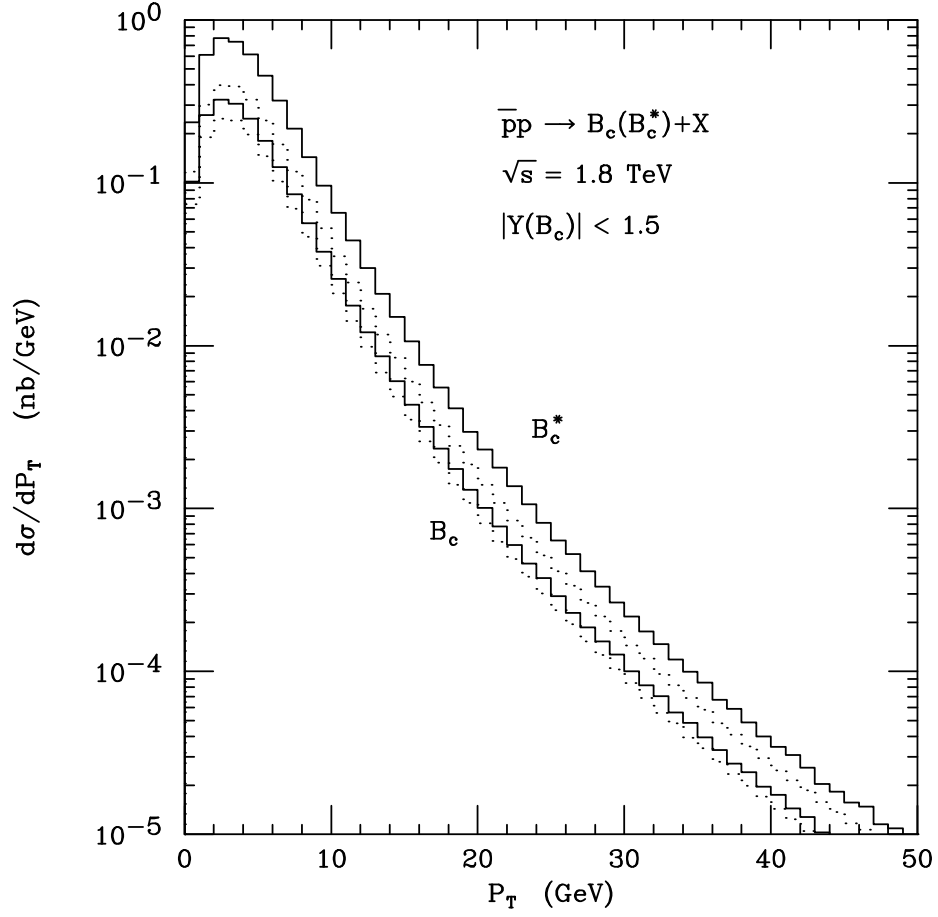


Fig. 1 The  $P_T$  distributions for  $B_c$  and  $B_c^*$  meson production at the Tevatron energy  $\sqrt{s} = 1.8 \text{ TeV}$ . The solid and the dotted lines correspond to the full  $\alpha_s^4$  calculation and the fragmentation approximation, respectively.

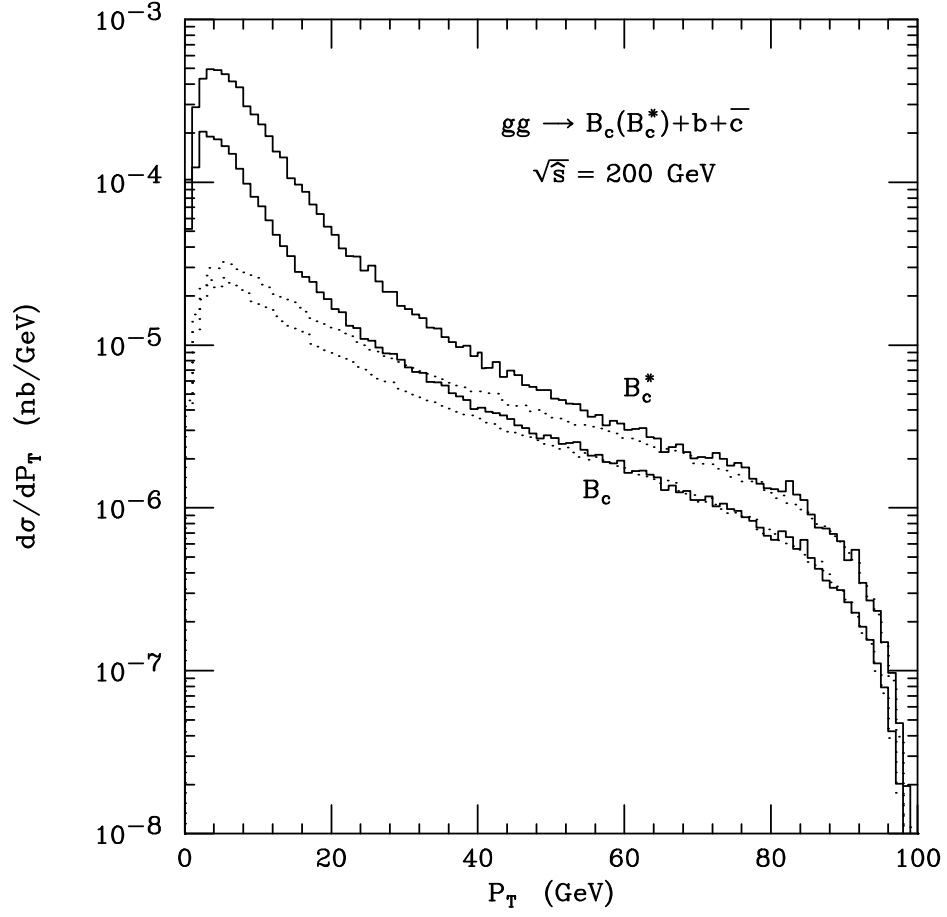


Fig. 2 The  $P_T$  distributions of the  $B_c$  and  $B_c^*$  meson for the subprocess with  $\sqrt{\hat{s}} = 200 \text{ GeV}$ . The solid and the dotted lines correspond to the full  $\alpha_s^4$  calculation and the fragmentation approximation, respectively.

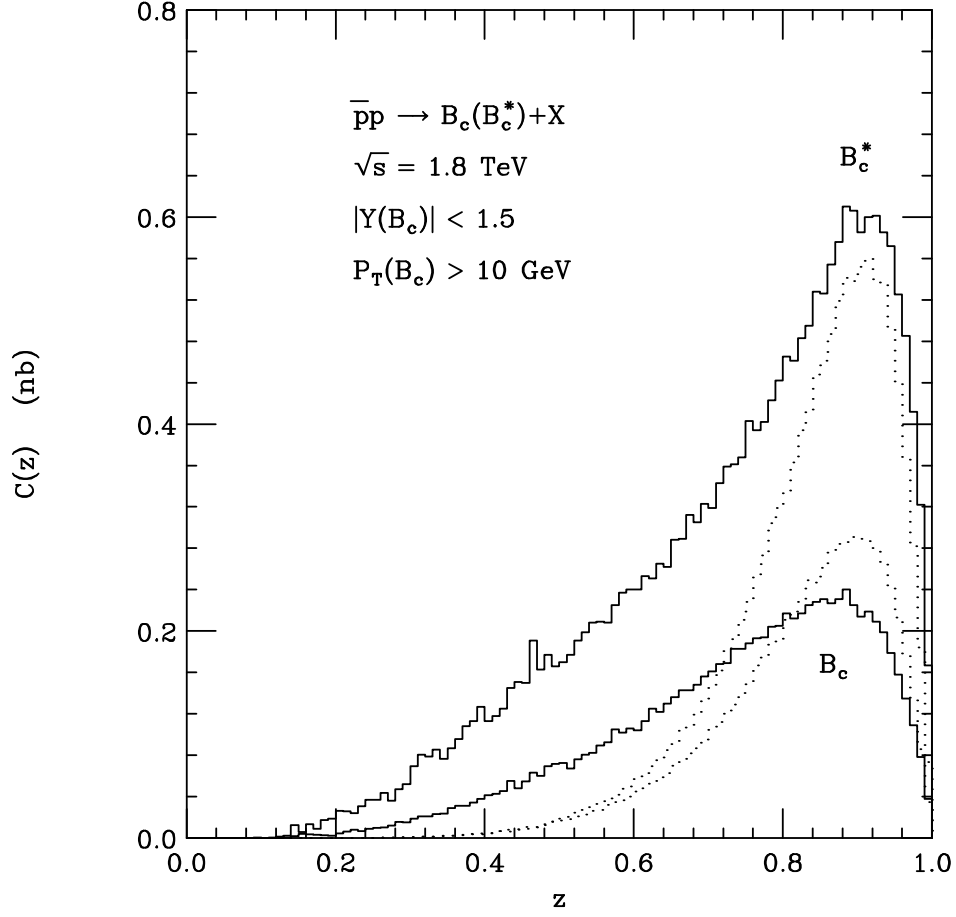


Fig. 3 The  $z$  distributions  $C(z)$  of the  $B_c$  and  $B_c^*$  at the Tevatron energy  $\sqrt{s} = 1.8$  TeV. The solid lines are the full  $\alpha_s^4$  calculation and the dotted lines are the fragmentation approximation with the cut  $P_T > 10 \text{ GeV}$

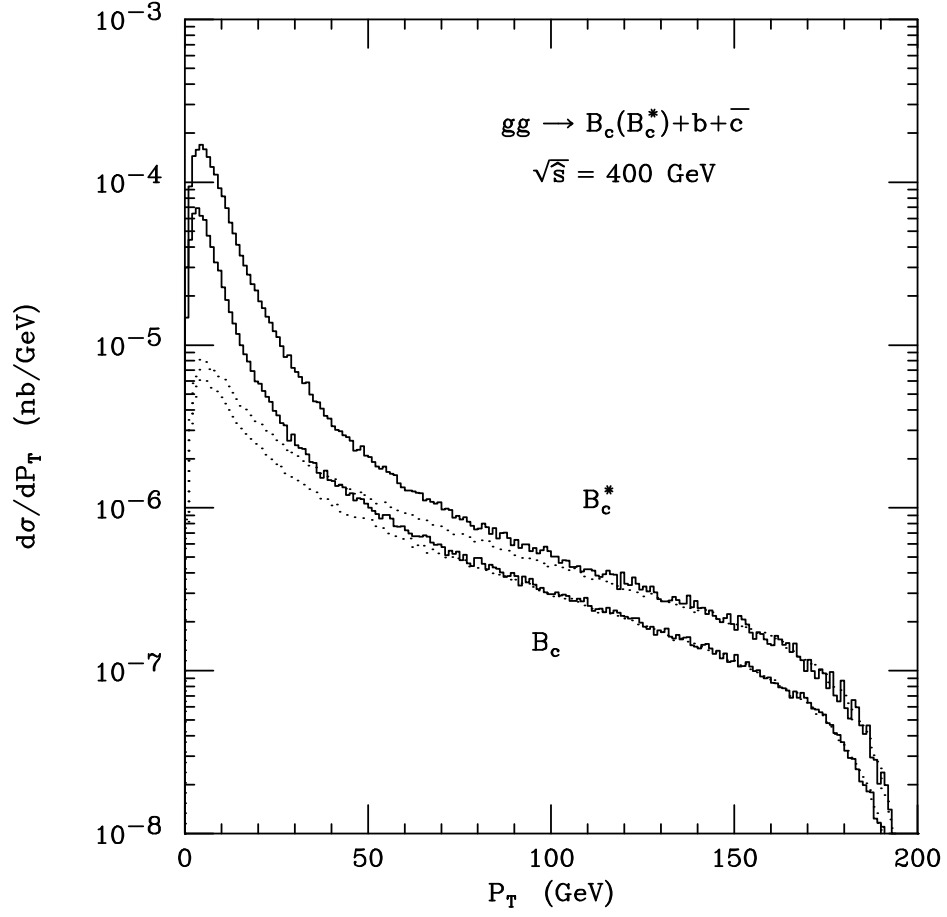


Fig. 4 The  $P_T$  distributions of the  $B_c$  and  $B_c^*$  meson for the subprocess with  $\sqrt{\hat{s}} = 400 \text{ GeV}$ . The solid and the dotted lines correspond to the full  $\alpha_s^4$  calculation and the fragmentation approximation, respectively.